

110. (Sixth problem of **Cluster 1**)

Both part 1 and part 2 of this problem involve uniformly accelerated motion, but at different rates  $a_1$  and  $a_2$ . We take the coordinate origin at point  $A$  and direct the positive axis towards  $B$  and  $C$ . In these terms, we are given  $x_A = 0$ ,  $x_C = 1300$  m,  $v_A = 0$ , and  $v_C = 50$  m/s. Further, the time-duration for each part is given:  $t_1 = 20$  s and  $t_2 = 40$  s.

- (a) We have enough information to apply Eq. 2-17 ( $\Delta x = \frac{1}{2}(v_0 + v)t$ ) to parts 1 and 2 and solve the simultaneous set:

$$\begin{aligned} x_B - x_A &= \frac{1}{2}(v_A + v_B)t_1 &\implies & x_B = \frac{1}{2}v_B(20) \\ x_C - x_B &= \frac{1}{2}(v_B + v_C)t_2 &\implies & 1300 - x_B = \frac{1}{2}(v_B + 50)(40) \end{aligned}$$

Adding equations, we find  $v_B = 10$  m/s.

- (b) The other unknown in the above set of equations is now easily found by plugging the result for  $v_B$  back in:  $x_B = 100$  m.
- (c) We can find  $a_1$  a variety of ways, using the just-obtained results. We note that Eq. 2-11 is especially easy to use.

$$v = v_0 + a_1 t_1 \implies 10 = 0 + a_1(20)$$

This leads to  $a_1 = 0.50$  m/s<sup>2</sup>.

- (d) To find  $a_2$  we proceed as just as we did in part (c), so that Eq. 2-11 for part 2 becomes  $50 = 10 + a_2(40)$ . Therefore, the acceleration is  $a_2 = 1.0$  m/s<sup>2</sup>.